Roll No: $\square$
BTECH
(SEM VI) THEORY EXAMINATION 2021-22
DESIGN AND ANALYSIS OF ALGORITHM
Time: 3 Hours
Total Marks: 100
Note: Attempt all Sections. If you require any missing data, then choose suitably.

## SECTION A

1. Attempt all questions in brief.

| Qno | Questions | CO |
| :--- | :--- | :--- |
| (a) | Explain the reason behind the call of Heapify procedure only on first <br> half elements of the given array while building a heap. | 1 |
| (b) | State the recurrence relation of Tower of Hanoi problem and solve it. | 1 |
| (c) | Discuss the properties of Binomial Trees. | 2 |
| (d) | Prove that a RB tree with n internal nodes has height atmost 2lg(n+1). | 2 |
| (e) | Discuss that why a shortest path cannot contain a cycle? | 3 |
| (f) | Differentiate between adjacency list and adjacency matrix <br> representation of graphs. | 3 |
| (g) | What is branch and bound technique? | 4 |
| (h) | Differentiate between Dynamic Programming and Divide \& Conquer <br> approach. | 4 |
| (i) | Write down complexity of naïve string matching algorithm. | 5 |
| (j) | Differentiate between NP Hard and NP Complete problems. | 5. |

## SECTION B

2. Attempt any three of the following:
$10 * 3=30$

| Qno | Questions | CO |
| :--- | :--- | :--- |
| (a) | Illustrate the working of the counting sort algorithm on array A: $\{2,0$, <br> $2,3,5,7,6,3,0,2,1,3\}$. | 1 |
| (b) | Show the final tree after inserting the following keys 22, 23, 44, 16, <br> 43, 26, $11,25,36,33,18$, in initially empty R-B tree in same sequence. | 2 |
| (c) | Define minimum cost spanning tree. Explain Prim's algorithm for <br> minimum spanning tree of a graph. Also write its Time-Complexity. | 3 |
| (d) | Illustrate the concept of backtracking on following sum-of-subset <br> problem, $n=4$, Sum i.e. $m=13$, and $w t_{1}=3, w t_{2}=4, w t_{3}=$ <br> $5, w t_{4}=7$ and $w t_{5}=8$. by building the search tree. | 4 |
| (e) | What is an approximation algorithm? What is meant by P(n) <br> approximation algorithms? Discuss approximation algorithm for <br> vertex cover problem. | 5 |

## SECTION C

3. Attempt any one part of the following:
$10 * \mathbf{1}=\mathbf{1 0}$

| Qno | Questions | CO |
| :--- | :--- | :--- |
| (a) | Write Merge sort algorithm and discuss its time complexity. | 1 |
| (b) | Apply quick sort to sort the keys as $12,13,10,5,7,3,2,17,23,16 . ~ A l s o ~$ <br> write its algorithm and discuss the running time of the quick sort. | 1 |

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4. Attempt any one part of the following: $\quad 10 \boldsymbol{*}=\mathbf{1 0}$

| Qno | Questions | CO |
| :--- | :--- | :--- |
| (a) | Illustrate the concept of trie data structure by constructing trie after <br> inserting following strings, "string, sting, streak, steak, stride, step, <br> steep," in order and then delete "step, streak" in order. | 2 |
| (b) | Write the characteristics of a B-Tree of degree t. Create B-Tree of t=3 <br> from the following lists of data items: $20,30,35,85,10,55,60,25$, <br> $5,65,70,75,15,40,50,90,45$. | 2 |

5. Attempt any one part of the following:
$10 * 1=10$

| Qno | Questions | CO |
| :--- | :--- | :--- |
| (a) | Define a Knapsack Problem and describe its formulation. Find the <br> optimal solution by using Greedy Method to Knapsack Instance $\mathrm{n}=5$, <br> w $=[20,30,40,10,7], \mathrm{P}=[700,800,900,100,600]$ and Capacity (C) of <br> Knapsack is 80. | 3 |
| (b) | Show all steps of Strassen's matrix multiplication algorithm using <br> suitable example. | 3 |

6. Attempt any one part of the following:
$10 * 1=10$

| Qno | Questions | CO |
| :--- | :--- | :--- | :--- |
| (a) | Define dynamic programming. How this approach different from <br> recursion? Explain with example. | 4 |
| (b) | Design an algorithm based upon dynamic programming for Longest <br> Common Subsequence(LCS) and then calculate LCS of sequence $\mathrm{X}=$ <br> $<\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{B}, \mathrm{D}, \mathrm{A}, \mathrm{B}>$ and $\mathrm{Y}=\angle \mathrm{B}, \mathrm{D}, \mathrm{C}, \mathrm{A}, \mathrm{B}, \mathrm{A}>$. | 4 |

7. Attempt any one part of the following:
$10 * 1=10$

| Qno | Questions | CO |
| :--- | :--- | :--- |
| (a) | Calculate the spurious hits in the text T $=3141592653589793$, pattern <br> $\mathrm{P}=26$ and working modulo $\mathrm{q}=11$, using Rabin-Karp string matching <br> algorithm after writing algorithm for the same. | 5 |
| (b) | Demonstrate the concept of FFT (Fast Fourier Transformation) with <br> the help of an example. | 5 |

